

Wireless Network Pricing

Chapter 3: Economics Basics

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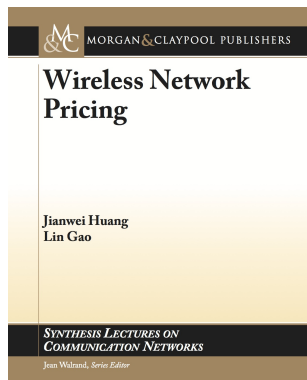
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The Book



- E-Book **freely** downloadable from NCEL website: <http://ncel.ie.cuhk.edu.hk/content/wireless-network-pricing>
- Physical book available for purchase from Morgan & Claypool (<http://goo.gl/JFGLai>) and Amazon (<http://goo.gl/JQKaEq>)

Chapter 3: Economics Basics

What is Economics?

Definition (Economics)

Economics is the study of how individuals and groups make decisions with **limited resources** as to best satisfy their wants, needs, and desires.

Firm and Consumer

- Follow the convention of economics, and use the terms “**firm**” and “**consumer**”
 - ▶ Example of firm: wireless service provider, wireless spectrum owner;
 - ▶ Example of consumer: wireless user, lower tier wireless service provider.

Definition (Firm)

A firm is an organization involved in the **production** and **trade** of goods, services, or both to consumers.

Definition (Consumer)

A consumer is a person or group of people, such as a household, who are the **final users** of products or services.

Examples: Economics



Ballard Farmers' Market (source: Internet)

Examples: Economics



Sao Paulo Stock Exchange (source: Internet)

Examples: Economics



Christie's Auction (source: Internet)

Section 3.1: Supply and Demand

Supply and Demand

- **Supply** and **Demand** in a market are both functions of **market prices**.
- Demand (of consumers) often **decreases** with prices, as consumers have less incentives to purchase under higher prices.
- Supply (of firms) often **increases** with prices, as firms have more incentives to produce under higher prices.

Market Demand Function

- **Example:** A consumer subscribes to a wireless cellular data plan.
 - ▶ Consumer's demand is 50 Gigabytes, if the price is \$1 Per Gigabyte;
 - ▶ Consumer's demand is 1.5 Gigabytes, if the price is \$20 Per Gigabyte.

Price Per Gigabyte	Wireless Data Demanded Per Month
\$1	50 Gigabytes
\$2	22 Gigabytes
\$10	4 Gigabytes
\$20	1.5 Gigabytes

Table: A consumer's monthly data demand vs the data price

Market Demand Function

- **Market Demand Function:** The relationship between the aggregate demand (of all consumers) and the market price.

Definition (Market Demand Function)

The **market demand function** $D(\cdot)$ characterizes the relationship between the total demand quantity Q_d and the product price P as follows:

$$Q_d = D(P)$$

Market Demand Function

- Illustration of **Market Demand Function**

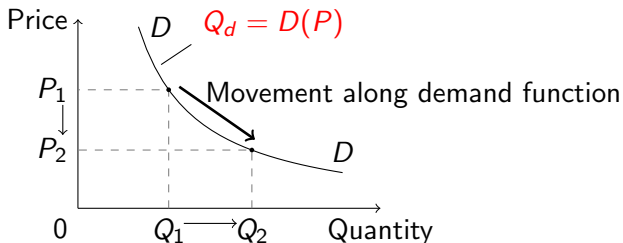


Figure: The market demand function $Q_d = D(P)$. When the price decreases from P_1 to P_2 , the demand increases from Q_1 to Q_2 .

Market Demand Function

- Market demand function itself may **shift** due to
 - ▶ the change of consumers' income;
 - ▶ the price change of other products;
 - ▶ the change of consumers' tastes;

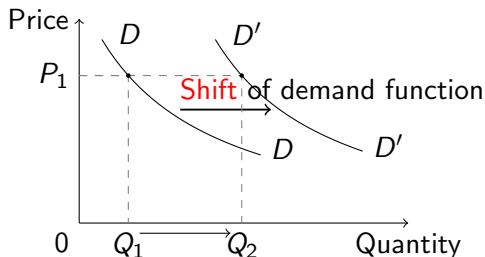


Figure: The shift of market demand function from $Q_d = D(P)$ to $Q'_d = D'(P)$. For example, under the same price P_1 , the demand changes from Q_1 to Q_2 .

Market Supply Function

- **Market Supply Function:** The relationship between the aggregate supply (of all firms) and the market price.

Definition (Market Supply Function)

The **market supply function** $S(\cdot)$ characterizes the relationship between the total supply quantity Q_s and the product price P as follows

$$Q_s = S(P)$$

Market Supply Function

- Illustration of **Market Supply Function**

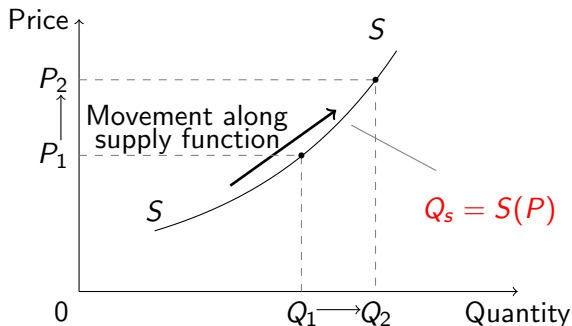


Figure: The market supply function $Q_s = S(P)$. When the price increases from P_1 to P_2 , the supply increases from Q_1 to Q_2 .

- Market supply function itself may **shift** when the price of a raw material (used for production) or the production technology changes.

Market Equilibrium

- **Market Equilibrium**: A market **stable** state under which the market is unlikely to change.
 - ▶ A prediction of how the actual market will look.
- A market (or market price) is **unstable**, when
 - ▶ The aggregate demand is **higher** than the aggregate supply, as consumers are willing to pay more to secure the limited supply (hence the market price will increase);
 - ▶ The aggregate demand is **lower** than the aggregate supply, as firms are willing to charge less to attract the limited demand (hence the market price will decrease);

Market Equilibrium

- Illustration of **Market Equilibrium**
 - ▶ When either market demand or supply function shifts due to factors other than the price, market equilibrium will change accordingly.

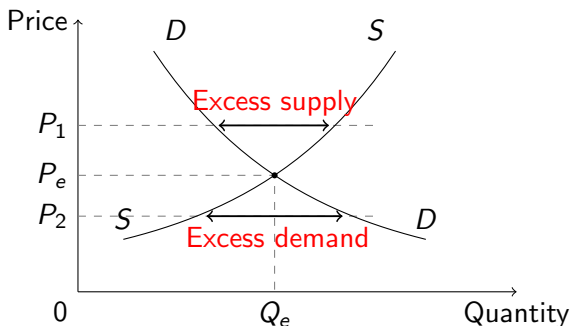


Figure: The market equilibrium price P_e and equilibrium quantity Q_e .

Market Equilibrium

Definition (Market Equilibrium)

At the **market equilibrium**, the aggregate demand equals the aggregate supply.

- Market equilibrium price P_e and the aggregate demand/supply Q_e :

$$Q_e = D(P_e) = S(P_e)$$

Section 3.2: Consumer Behavior

Consumer Behavior

- Focus on the **behavior** of a particular consumer, and understand how the market demand function $Q_d = D(P)$ is derived from the consumer's utility maximization behaviour.
- **Basic Concepts**
 - ▶ Market Basket
 - ▶ Consumer Utility
 - ▶ Indifference Curve
 - ▶ Budget Constraint
 - ▶ Consumer Demand Function
 - ▶ Price Elasticity

Market Basket

- How a consumer evaluates the **benefit** of consuming products?
 - ▶ For example, how would a consumer evaluate the satisfaction level of watching a 60-minute action movie and playing 30 minutes of video games on his iPad?

Definition (Market Basket)

A **market basket** (also known as **commodity bundle**) specifies the quantity of different products.

- For example, watching a 60-minute movie and playing 30 minutes of game can be represented by the **market basket (60, 30)**.

Consumer Utility

- **Consumer Utility Function**: Characterize a consumer's **satisfaction level** of consuming a certain market basket (x, y) , i.e.,

$$U = U(x, y)$$

Indifference Curve

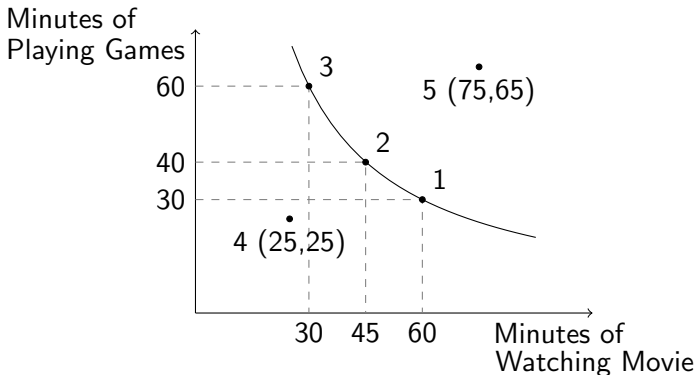
- **Indifference Curve**: Characterizes how a consumer **trades off** two different baskets of products

Definition (Indifference Curve)

An **indifference curve** represents a set of market baskets where the consumer's utilities are the same.

Indifferent Curve

- Illustration of **Indifference Curve**
 - ▶ Basket 1 (60, 30), basket 2 (45, 40), and basket 3 (30, 60) are on the same indifference curve (benchmark);
 - ▶ Basket 5 (75, 65) is on an indifference curve with a higher utility;
 - ▶ Basket 4 (25, 25) is on an indifference curve with a lower utility.



Budget Constraint

Definition (Budget Constraint)

The **budget constraint** characterizes which market baskets are affordable to the consumer.

- **Example:** Watching one minute of movie will cost 1 unit of energy, and playing one minute of game will cost 2 units of energy. Then, the constraint of 100 units of energy leads to the budget constraint:

$$x + 2y \leq 100$$

- More generally,

$$P_x x + P_y y \leq I$$

- ▶ Here P_x and P_y are the unit prices, and I is the budget.

Budget Constraint

- Illustration of Budget Constraint

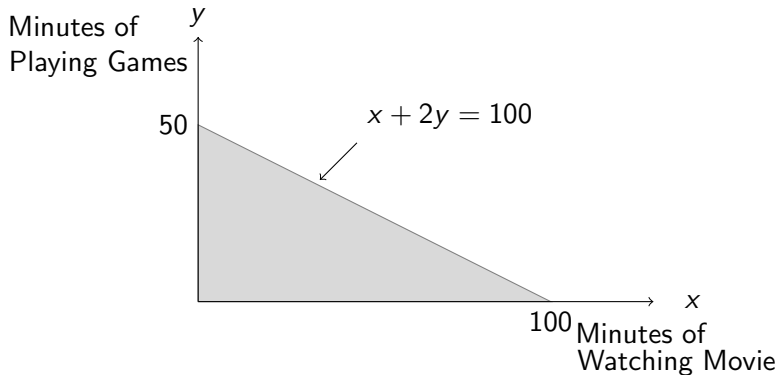


Figure: Illustration of budget constraint $x + 2y \leq 100$.

Consumer Consumption Problem

- How a consumer decides **which market basket to purchase?**
- **Objective:** Want to maximize its utility subject to the budget constraint.
- Geometrically, the consumer's optimal choice is the **highest indifference curve** that “touches” the budget constraint.

Consumer Consumption Problem

- Illustration of **Consumer's Optimal Choice**
 - ▶ $U_1 < U_2 < U_3$ are three indifference curves;
 - ▶ Budget constraint is $x_c + 2y_c \leq 100$;

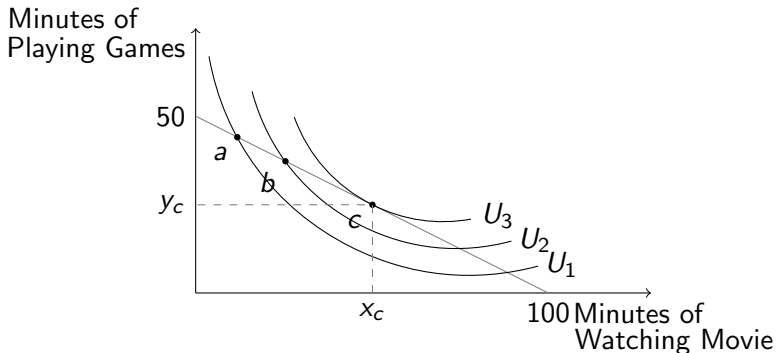


Figure: Consumer's optimal market basket choice is **basket c**.

Consumer Consumption Problem

- **Consumer's Optimal Choice** in the previous figure
 - ▶ The derivative of the indifference curve with utility U_3 at basket c equals to the slope of the budget constraint at basket c , i.e., the budget constraint is the tangent line to the indifference curve at basket c ,

$$\left. \frac{\Delta y}{\Delta x} \right|_{U(x,y)=U_3, (x,y)=(x_c, y_c)} = -\frac{P_x}{P_y}$$

- ▶ Recall that the budget constraint is

$$P_x x + P_y y \leq I$$

- ▶ The lefthand side is called **marginal rate of substitution (MRS)**, representing how much the consumer is willing to tradeoff one product with the other product.
- ▶ In general MRS is **not a constant** on a particular indifference curve.

Consumer Demand Function

- **Consumer Demand Function:** Characterizes how a consumer's demand of a product changes with the price of that product.
- **Market demand function:** simply the summation of all consumers' demand functions in the same market.

Consumer Demand Function

- **Example:** Assume that there are three games on iPad.
 - ▶ The consumer can choose **one game** to play and **watching movie**.
 - ▶ The energy prices of these three games are 1/min, 2/min, and 4/min, respectively. The energy price of watching movie is 1/min.

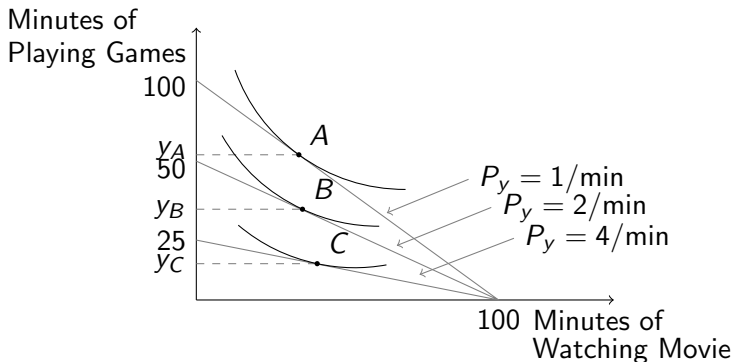


Figure: Consumer's optimal choices: A for 1/min, B for 2/min, C for 4/min.

Consumer Demand Function

- Connecting the consumer's optimal choices under different energy prices will lead to the demand function.

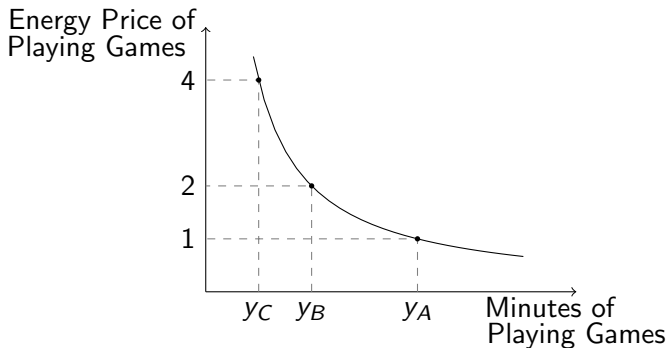


Figure: Consumer's demand function (for playing games) as a function of the energy price.

Price Elasticity

- **Price Elasticity:** Characterize the **sensitivity** of demand in term of price, i.e., how fast the demand changes with the price.
- **Example:** Cellular Wireless Data Usage.
 - ▶ A college student might be very price sensitive, and will dramatically decrease the monthly data usage if the price increases;
 - ▶ A business consumer might be much less sensitive and not even notice the change of price until several months later.

Price Elasticity

Definition (Price Elasticity)

The **price elasticity of demand** measures the ratio between the percentage change of demand and the percentage change of price, i.e.,

$$E_d = \frac{\% \text{ change in demand}}{\% \text{ change in price}} = \frac{\Delta Q_d / Q_d}{\Delta P / P}$$

Price Elasticity

- Illustration of **Price Elasticity E_d**
 - ▶ $E_d < 0$ due to the downward sloping of the demand curve.

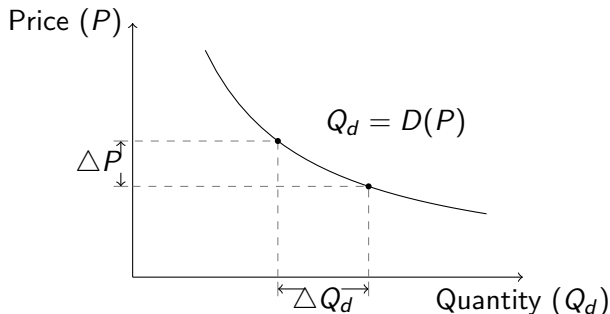


Figure: The change of demand ΔQ_d due to the change of price ΔP .

Price Elasticity

- When the demand function Q_d is **differentiable**, then

$$E_d = \frac{P}{Q_d} \cdot \frac{\partial Q_d}{\partial P}$$

- **Three Demand Types:**

- ▶ **Elastic demand:** the demand changes significantly with the price and $E_d < -1$.
- ▶ **Inelastic demand:** the demand is not sensitive to price and $-1 < E_d < 0$.
- ▶ **Unitary elastic demand:** $E_d = -1$.

Section 3.3: Firm Behavior

Firm Behavior

- Focus on the **behavior** of a particular firm, and understand how the market supply function $Q_s = S(P)$ is derived from the firm's cost minimization behavior.
- **Basic Concepts**
 - ▶ Marginal Cost
 - ▶ Competitive Firm

Firm Cost

- **Total Cost** of A firm:
 - ▶ **Fixed cost**: the cost independent of the quantity produced.
 - ▶ **Variable cost**: the cost depending on the production quantity.

Definition (Firm Cost)

The **total production cost** of a firm includes both the fixed cost F and variable cost $V(q)$, i.e.,

$$C(q) = F + V(q)$$

where q is the production quantity.

Marginal Cost

- **Marginal Cost:** Characterize how the total cost $C(q)$ changes when the firm changes the production quantity q .

Definition (Marginal Cost)

The **marginal cost** measures how the total cost changes with the production quantity, i.e.,

$$MC(q) = \frac{\text{change in total production cost}}{\text{change in production quantity}} = \frac{\Delta C(q)}{\Delta q} = \frac{\Delta V(q)}{\Delta q}$$

- ▶ The fixed cost F does **not** affect the computation of marginal cost.
- ▶ If the variable cost function $V(q)$ is **differentiable**, then

$$MC(q) = \frac{\partial C(q)}{\partial q} = \frac{\partial V(q)}{\partial q}$$

Competitive Firm

Definition (Competitive Firm)

A **competitive firm** is **price-taking** and acts as if the market price is **independent** of the quantity produced and sold by the firm.

- The above definition reflects the reality when the firm faces **many competitors** in the same market.
- Each firm's production decision is unlikely to significantly change the total quantity available in the market, and thus will **not** significantly affect the market price.

Competitive Firm Profit

- **Total Profit** of a Competitive Firm
 - ▶ q : the firm's production quantity;
 - ▶ P : the market price **independent** of the quantity q ;
 - ▶ F : the firm's fixed cost **independent** of the quantity q ;
 - ▶ $V(q)$: the firm's variable cost **depending** on the quantity q ;

Definition (Profit of Competitive Firm)

A competitive firm's **total profit** is the difference between the total revenue and total cost, i.e.,

$$\pi(q) = P \cdot q - V(q) - F$$

Competitive Firm Optimal Decision

- A Competitive **Firm's Decision Problem**: Decide the optimal production quantity q that maximize its total profit:

$$\pi(q) = P \cdot q - V(q) - F$$

- The **Firm's Optimal Quantity** Choice q^* is given by:

$$P = \frac{\partial V(q)}{\partial q} = MC(q)$$

Section 3.4: Chapter Summary

Key Concepts

- Supply and Demand
- Consumer Behavior Model
- Firm Behavior Model

Extended Reading

<http://ncel.ie.cuhk.edu.hk/content/wireless-network-pricing>